

Forman Christian College Lahore (A Chartered University) Department of Mathematics Fall 2021

Dr. Shabnam Malik

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Course Information:

Calculus and Analytic Geometry, MATH 111 (B), 3 credits, Class Room: S-412 Lectures Time: Monday, Wednesday & Friday (02:00 - 02:50) Prerequisite: MATH-101 / A-level / FSc pre-engineering Text Book: "Calculus" by Howard Anton, Irl Bivens and Stephen Davis, 10th edition https://www.academia.edu/34762815/Calculus_10th_edition_H_Anton Reference Book: "Calculus" by Thomas and Finney, 13th edition.

Course Description: This a supporting course and compulsory course for computer science major. The focus of this course is the study of the inverse relationship that exists between differential and integral calculus.

Course contents include: Fundamentals of functions, limits and continuity, derivatives, problem solving using differentiation (extreme value problems, curve sketching, related rates problems, etc), integrations techniques, Fundamental Theorem of Calculus, computation of areas and volumes by slicing, volumes of revolution and surface areas of revolution, infinite series and convergence tests and Taylor's series.

Course Objectives: The course will help students to:

- Learn the fundamentals of calculus along with its application to interesting problems in science and engineering and develop an appreciation of calculus as a coherent body of knowledge and as a human accomplishment.
- Recall the fundamentals of functions.
- Understand the fundamental concept of limit, and how it is computed.
- Understand the concept of rate of change in the form of derivative and to evaluate various differentiation techniques.
- Understand how derivative helps us with optimization, rates of change, and the shape of a graph.
- Get familiar with the techniques of evaluating integrals.
- Understand the relationship between the derivative and the definite integral as expressed in the Fundamental Theorem of Calculus, and relate definite integral to area.
- Understand the application of integration.
- Understand the infinite series, convergence test and Taylor series.

Learning Outcomes: Upon successful completion of this course, the student will be able

to:

- Understand the basics of function, its domain, range, intercepts, and graph, functions operations, composition function, inverse function, and function transformations.
- Familiar with basics of conic section: circle, ellipse, parabola and hyperbola.
- Familiar with the notion of limit and compute limits by graphs, compute limits of various functions, such as polynomials, rational functions, functions involving radicals, piecewise functions, and trigonometric functions, and know the concepts of continuity.
- Know the limit definition of derivative and how to evaluate derivatives by definition.
- Know the basic rules of differentiation and use them to find derivatives of products and quotients.
- Evaluate the derivatives of power, trigonometric, exponential, logarithmic and inverse trigonometric functions, and know the chain rule and use it to find derivatives of composite functions.
- Know implicit and logarithmic differentiation.
- Familiar with application of derivatives such as, related rates, to find limits in indeterminate forms by a repeated use of L'H^opital's rule, to find absolute extrema on a closed interval, to find relative extrema using the first derivative test, to find critical points and intervals where a function is increasing or decreasing, to find inflection points and intervals where a function is concave up or concave down, to use the second derivative test to find local extrema, and to solve applied optimization problems.
- Understand the concept of indefinite integral as anti-derivative, and know standard indefinite integrals and basic rules of indefinite integration.
- Evaluate integrals by substitution and by a repeated use of integration by parts.
- Evaluate integrals of rational functions by partial fractions.
- Understand the concept of definite integral and Fundamental Theorems of Calculus, and know the basic properties of definite integrals and that how to evaluate definite Integrals.
- Use integration to find the area under the curve, the area between two curves, the length of a plane curve, volume by slicing, the volumes of solids obtained by rotating the curve.
- Understand infinite series and convergence Tests, and Taylors Series

Course Requirements:

- Attendance: Students are expected to attend every class. Student whose attendance is less than 60% won't be allowed to take the final exam. Students must arrive at class on time, should remain in class for the entire class period and mobile phone should be switched off or on silence. Note that there is 5 marks for attendance and behaviour, if a student arrives more than 10 minutes late or leaves class during lecture or uses mobile in class, he/she will be marked absent.
- Assessment: Course assessment will be through quizzes, attendance and behavior, assignments, midterm, and final exam. Quizzes, mid term exam and final exam will be conducted on campus for all students. Assignments will be conducted on Moodle along with its viva on Zoom or in person. There is no make up for missed quizzes but best 3 out of 4 will be counted. Make up for midterm and final exam is possible only under extremes cases if student provides strong documentary evidence within three days. In case of make up exam there will be a 0-20% deduction in marks depending upon case to case basis.
- Academic dishonesty or cheating: Academic dishonesty or cheating will result in zero points and will be referred to AIC (Academic Integrity Committee) at FCC for necessary action.

Grades	Quality Points	Numerical Value
А	4.00	93-100
A-	3.70	90-92
B+	3.30	87-89
В	3.00	83-86
В-	2.70	80-82
C+	2.30	77-79
С	2.00	73-76
C-	1.70	70-72
D+	1.30	67-69
D	1.00	60-66
F	0.00	59 or below

<u>Course Evaluation</u>: Grading will be based on following criteria:

Attendance and Behaviour	05 %
Assignments (2)	10 %
Quizzes (4)	15 %
Mid Term	30 %
Final Exam	40 %

Week	Topics	Assessments
1	Discussion of Course plan and Overview of Course Syllabus	
Nov 01, 03, 05	Review of Basic Concepts	
	 Functions, Types and Their Domains 	
	 Operations on Functions, Composition of Functions, Inverse 	
	Function	
	 Graphing the Basic Functions 	
2	Brief Review of Conic Section	
Nov 08, 10, 12	 Introduction to Circle, Ellipse, Parabola and Hyperbola 	
00, 10, 12	<u>Limits</u>	
	 Finding Limits by Graphs 	
	 Computational Techniques of Limits 	
3	 Limits of Piecewise Functions 	Quiz-1
Nov 15, 17, 19	 Limits of Trigonometric Function 	Nov 17 (Wed)
-, , -	 Finding Limits at Infinity Using Graphs 	
	 Computing Limits at infinity 	
4	✤ Continuity	
Nov 22, 24, 26	<u>Derivatives</u>	
, , -	 Limit Definition of Derivative, Differentiability, Evaluating 	
	Derivatives by Definition	
5	 Techniques of Differentiation, The Product and Quotient rules 	
Nov 29	 Derivative of Trigonometric functions 	
Dec 01, 03	 The Chain Rule, Higher Derivatives 	
6	 Derivative of Exponential and Logarithmic Functions 	Quiz-2
Dec 06, 08, 10	 Logarithmic Differentiation 	Dec 08 (Wed)
00, 00, 10	 Implicit Differentiation 	

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7	Application of Derivatives:	Assignment 1
Dec 13, 15, 17	 Related Rates 	
13, 13, 17	 L'Hopital's Rule; Indeterminate Forms 	
8	MID TERM EXAM	MID TERM
Dec 20		Dec 20 (Mon)
9	 Increasing and Decreasing Curves 	
Jan 03, 05, 07	 First and Second Derivative test 	
00, 00, 01	 Maxima and Minima Problems 	
10	 Concavity and Curve Sketching 	
Jan 10, 12, 14	 Applied Optimization Problems 	
11	Integrals:	
Jan	 Introduction to Anti-derivative, The Indefinite Integral and 	
17, 19, 21	Techniques of Integration	
	 Integration by Parts 	
	 Integration by Trigonometric Substitution 	
12	 Integrating Rational Functions by Partial Fractions 	Quiz-3
Jan	 Definite Integrals, Fundamental Theorems of Calculus, and 	Jan 26 (Wed)
24, 26, 28	evaluating Definite Integrals	
13	Application of Integrals:	
Jan 31 Feb 02, 04	 Computation of Areas 	Assignment 2
1 05 02, 04	 Length of a Plane Curve 	
14	Volume by Slicing	
Feb 07, 09, 11	 Volume of Solids of Revolution (Disk and Washer Method) 	
15	 Surface Areas of Revolution 	
Feb	Infinite Series:	Quiz-4
14, 16, 18	 Infinite Series and Convergence Tests 	Feb 16 (Wed)
	 ⋆ Taylors Series 	
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